

Evidence for a $J/\psi p\bar{p}$ Pauli Strong Coupling ?

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The couplings of charmonia and charmonium hybrids (generically Ψ) to $p\bar{p}$ are of great interest in view of future plans to study these states using an antiproton storage ring at GSI. These low to moderate energy $\Psi p\bar{p}$ couplings are not well understood theoretically, and currently must be determined from experiment. In this letter we note that the two independent Dirac (γ_μ) and Pauli ($\sigma_{\mu\nu}$) $p\bar{p}$ couplings of the J/ψ and ψ' can be constrained by the angular distribution of $e^+e^- \rightarrow (J/\psi, \psi') \rightarrow p\bar{p}$ on resonance. A comparison of our theoretical results to recent unpolarized data allows estimates of the $p\bar{p}$ couplings; in the better determined J/ψ case the data is inconsistent with a pure Dirac (γ_μ) coupling, and can be explained by the presence of a $\sigma_{\mu\nu}$ term. This Pauli coupling may significantly affect the cross section of the PANDA process $p\bar{p} \rightarrow \pi^0 J/\psi$ near threshold. There is a phase ambiguity that makes it impossible to uniquely determine the magnitudes and relative phase of the Dirac and Pauli couplings from the unpolarized angular distributions alone; we show in detail how this can be resolved through a study of the polarized reactions.

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I. INTRODUCTION

Charmonium is usually studied experimentally through e^+e^- annihilation or hadronic production, notably in $p\bar{p}$ annihilation. The $p\bar{p}$ annihilation process was employed by the fixed target experiments E760 and E835 at Fermilab, which despite small production cross sections succeeded in giving very accurate results for the masses and total widths of the narrow charmonium states J/ψ , ψ' , χ_1 and χ_2 . A future experimental program of charmonium and charmonium hybrid production using $p\bar{p}$ annihilation that is planned by the PANDA collaboration [1] at GSI is one of the principal motivations for this study.

Obviously the strengths and detailed forms of the couplings of charmonium states to $p\bar{p}$ are crucial questions for any experimental program that uses $p\bar{p}$ annihilation to study charmonium; see for example the predictions for the associated production processes $p\bar{p} \rightarrow \pi^0 \Psi$ in Refs.[2, 3, 4]. (We use Ψ to denote a generic charmonium or charmonium hybrid state, and ψ if the state has

$J^{PC} = 1^{--}$.)

Unfortunately these low to moderate energy production reactions involve obscure and presumably rather complicated QCD processes, so for the present they are best inferred from experiment. In Ref.[4] we carried out this exercise by using the measured $p\bar{p}$ partial widths to estimate the coupling constants of the $J/\psi, \psi', \eta_c, \eta'_c, \chi_0$ and χ_1 to $p\bar{p}$, assuming that the simplest Dirac couplings were dominant. These $\Psi p\bar{p}$ couplings were then used in a PCAC-like model to give numerical predictions for several associated charmonium production cross sections of the type $p\bar{p} \rightarrow \pi^0 \Psi$.

In this paper we generalize these results for the J/ψ and ψ' by relaxing the assumption of γ_μ dominance of the $\psi p\bar{p}$ vertex. We assume a $\psi p\bar{p}$ vertex with both Dirac (γ_μ) and Pauli ($\sigma_{\mu\nu}$) couplings, and derive the differential and total cross sections for $e^+e^- \rightarrow \psi \rightarrow p\bar{p}$ given this more general vertex. Both unpolarized and polarized processes are treated.

A comparison of our theoretical unpolarized angular distributions to recent experimental J/ψ results allows estimates of both the Dirac and Pauli $J/\psi p\bar{p}$ couplings. There is a phase ambiguity that precludes a precise determination of the (complex) ratio of the Pauli and Dirac $J/\psi p\bar{p}$ couplings from the unpolarized data; we shall see that an importance interference effect between the Pauli and Dirac terms leads to a strong dependence of the unpolarized $p\bar{p} \rightarrow \pi^0 J/\psi$ cross section near threshold on the currently unknown phase between these terms.

Determining these couplings is evidently quite important for PANDA, and can be accomplished through stud-

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ies of the polarized process $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$. The angular distribution of the unpolarized, self-analyzing process $e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}$ may also provide complementary information regarding the closely related $J/\psi\Lambda\bar{\Lambda}$ vertex. Both of these processes should be accessible at the upgraded BES-III facility.

II. UNPOLARIZED CROSS SECTION

The Feynman diagram used to model this process is shown in Fig.1. We assume a vertex for the coupling of a generic 1^{--} vector charmonium state ψ to $p\bar{p}$ of the form

$$\Gamma_\mu^{(\psi p\bar{p})} = g\left(\gamma_\mu + \frac{i\kappa}{2m}\sigma_{\mu\nu}q_\nu\right). \quad (1)$$

In this paper m and M are the proton and charmonium mass, Γ is the charmonium total width, and we assume massless initial leptons. Following DIS conventions, q_ν is the four momentum transfer *from* the nucleon to the electron; thus in our reaction $e^+e^- \rightarrow p\bar{p}$ in the c.m. frame, we have $q = (-\sqrt{s}, \vec{0})$. The couplings g and κ are actually momentum dependent form factors, but since we only access them very close to the kinematic point $q^2 = M^2$ in the reactions $e^+e^- \rightarrow (J/\psi, \psi') \rightarrow p\bar{p}$, we will treat them as constants.

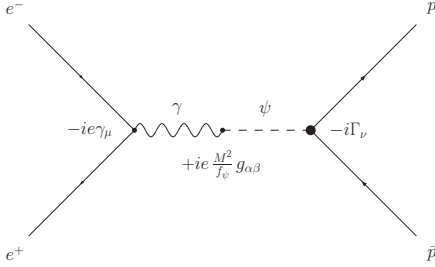


FIG. 1: The Feynman diagram assumed in this model of the generic reaction $e^+e^- \rightarrow \psi \rightarrow p\bar{p}$.

The unpolarized differential and total cross sections for $e^+e^- \rightarrow \psi \rightarrow p\bar{p}$ may be expressed succinctly in terms of the strong $\psi p\bar{p}$ Sachs form factors $\mathcal{G}_E = g(1 + \kappa s/4m^2)$ and $\mathcal{G}_M = g(1 + \kappa)$. Both \mathcal{G}_E and \mathcal{G}_M are complex above $p\bar{p}$ threshold, in part because phases are induced by $p\bar{p}$ rescattering. If we assume that the lowest-order Feynman diagram of Fig.1 is dominant, the phase of g itself is irrelevant, so here we take g to be real and positive. κ however has a nontrivial phase. We express this by introducing a Sachs form factor ratio, with magnitude $\rho \geq 0$ and phase χ ;

$$\mathcal{G}_E/\mathcal{G}_M \equiv \rho e^{i\chi}. \quad (2)$$

The corresponding relation between the Pauli coupling constant κ and this Sachs form factor ratio is

$$\kappa \equiv |\kappa| e^{i\phi_\kappa} = \frac{\rho e^{i\chi} - 1}{(M^2/4m^2 - \rho e^{i\chi})} \quad (3)$$

where we have assumed that we are on a narrow resonance, so we can replace s by M^2 .

We will first consider the unpolarized process $e^+e^- \rightarrow \psi \rightarrow p\bar{p}$, and establish what the differential and total cross sections imply regarding the $\psi p\bar{p}$ vertex. The unpolarized total cross section predicted by Fig.1 is

$$\langle\sigma\rangle = \frac{4\pi\alpha^2 M^4}{3f_\psi^2 s^2} \frac{(1 - 4m^2/s)^{1/2}}{[(s - M^2)^2 + \Gamma^2 M^2]} (2m^2|\mathcal{G}_E|^2 + s|\mathcal{G}_M|^2). \quad (4)$$

(We use angle brackets to denote a polarization averaged quantity.) Exactly on resonance (at $s = M^2$) this can be expressed in terms of the ψ partial widths

$$\Gamma_{\psi \rightarrow e^+e^-} = \frac{4\pi\alpha^2 M}{3f_\psi^2} \quad (5)$$

and

$$\Gamma_{\psi \rightarrow p\bar{p}} = \frac{(1 - 4m^2/M^2)^{1/2}}{12\pi M} (2m^2|\mathcal{G}_E|^2 + M^2|\mathcal{G}_M|^2), \quad (6)$$

which gives the familiar result

$$\langle\sigma\rangle|_{s=M^2} = \frac{12\pi}{M^2} B_{e^+e^-} B_{p\bar{p}}. \quad (7)$$

Here $B_{e^+e^-}$ and $B_{p\bar{p}}$ are the $\psi \rightarrow e^+e^-$ and $\psi \rightarrow p\bar{p}$ branching fractions.

Since the (unpolarized) $p\bar{p}$ width and total cross section on resonance involve only the single linear combination $(2m^2|\mathcal{G}_E|^2 + M^2|\mathcal{G}_M|^2)$, separating these two strong form factors requires additional information, such as the angular distribution. The unpolarized $e^+e^- \rightarrow \psi \rightarrow p\bar{p}$ differential cross section in the c.m. frame is given by

$$\left\langle \frac{d\sigma}{d\Omega} \right\rangle = \frac{\alpha^2 M^4}{4f_\psi^2 s^2} \frac{(1 - 4m^2/s)^{1/2}}{[(s - M^2)^2 + \Gamma^2 M^2]} \cdot \left[4m^2|\mathcal{G}_E|^2(1 - \mu^2) + s|\mathcal{G}_M|^2(1 + \mu^2) \right], \quad (8)$$

where $\mu = \cos(\theta_{c.m.})$. This angular distribution is often expressed as $1 + \alpha\mu^2$, where

$$\alpha = \frac{1 - (4m^2/s)|\mathcal{G}_E/\mathcal{G}_M|^2}{1 + (4m^2/s)|\mathcal{G}_E/\mathcal{G}_M|^2}. \quad (9)$$

Inspection of Eqs.(8,9) shows that one can determine the magnitude $\rho = |\mathcal{G}_E/\mathcal{G}_M|$ of the Sachs form factor ratio from the unpolarized differential cross section, but that the phase χ of $\mathcal{G}_E/\mathcal{G}_M$ is unconstrained.

The undetermined phase χ implies an unavoidable ambiguity in determining the magnitude and phase of the Dirac and Pauli $\psi p\bar{p}$ couplings g and κ from the unpolarized $e^+e^- \rightarrow (J/\psi, \psi') \rightarrow p\bar{p}$ angular distribution. We will discuss this ambiguity in the next section.

III. COMPARISON WITH EXPERIMENT

A. Summary of the data

Experimental values of α have been reported by several collaborations. The results for the J/ψ are

$$\alpha = \begin{cases} 1.45 \pm 0.56, & \text{MarkI [5]} \\ 1.7 \pm 1.7, & \text{DASP [6]} \\ 0.61 \pm 0.23, & \text{MarkII [7]} \\ 0.56 \pm 0.14, & \text{MarkIII [8]} \\ 0.62 \pm 0.11, & \text{DM2 [9]} \\ 0.676 \pm 0.036 \pm 0.042, & \text{BES [10].} \end{cases} \quad (10)$$

and for the ψ'

$$\alpha = \begin{cases} 0.67 \pm 0.15 \pm 0.04, & \text{E835 [11]} \\ 0.85 \pm 0.24 \pm 0.04, & \text{BES [12].} \end{cases} \quad (11)$$

For our comparison with experiment we use the statistically most accurate measurement for each charmonium state, and combine the errors in quadrature. This gives experimental estimates for α of 0.676 ± 0.055 and 0.67 ± 0.155 for the J/ψ and ψ' respectively.

B. Testing the pure Dirac hypothesis

We first examine these experimental numbers using the “null hypothesis” of no Pauli term, $\kappa = 0$, in which case $\alpha = (1 - r)/(1 + r)$, where $r = 4m^2/M^2$. This $\kappa = 0$ formula was previously given by Claudson, Glashow and Wise [13] and by Carimalo [14]; the value of α under various theoretical assumptions has been discussed by these references and by Brodsky and LePage [15], who predicted $\alpha = 1$. Fig.2 shows these two experimental values together with the pure Dirac (γ_μ) formula for α . The ψ' case is evidently consistent with a Dirac (γ_μ) $\psi' p\bar{p}$

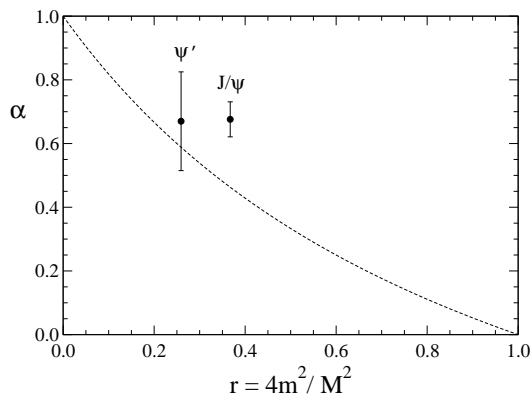


FIG. 2: The coefficient α observed in the unpolarized $e^+e^- \rightarrow (J/\psi, \psi') \rightarrow p\bar{p}$ angular distributions, together with the theoretical result $\alpha = (1 - r)/(1 + r)$ predicted by a pure Dirac (γ_μ) $\psi p\bar{p}$ coupling.

coupling at present accuracy, but the better determined J/ψ angular distribution is inconsistent with a pure Dirac $J/\psi p\bar{p}$ coupling at the 4σ level.

The discrepancy evident in Fig.2 may imply the presence of a Pauli term ($\kappa \neq 0$) in the $J/\psi p\bar{p}$ vertex. Inspection of our result for α in the general case (Eq.9) shows that one can certainly accommodate this discrepancy by introducing a Pauli term.

C. Determining $\rho = |\mathcal{G}_E/\mathcal{G}_M|$ from α

The dependence of the predicted α on ρ at the J/ψ mass (from Eq.9) is shown in Fig.3. The experimental value $\alpha = 0.676 \pm 0.055$ (shown) is consistent with the Sachs form factor magnitude ratio of

$$\rho = |\mathcal{G}_E/\mathcal{G}_M| = 0.726 \pm 0.074. \quad (12)$$

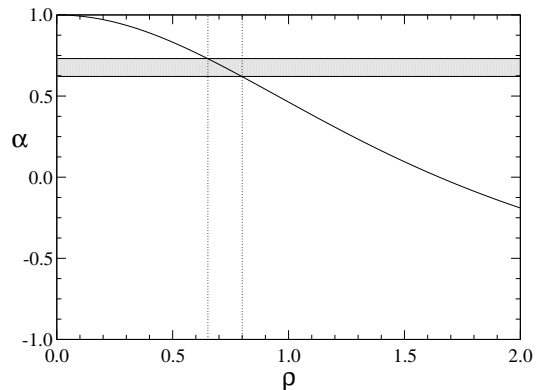


FIG. 3: The experimental value of the unpolarized $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$ angular coefficient, $\alpha = 0.676 \pm 0.055$ (shaded), and the resulting Sachs $J/\psi p\bar{p}$ strong form factor magnitude ratio $\rho = |\mathcal{G}_E/\mathcal{G}_M|$ (Eq.12).

In terms of ρ and χ this completes our discussion: Given the unpolarized angular distribution, one obtains a result for $\rho = |\mathcal{G}_E/\mathcal{G}_M|$ from Eq.9, but the phase χ of $\mathcal{G}_E/\mathcal{G}_M$ is undetermined. However one may ask the more fundamental question of what values of the Dirac and Pauli coupling constants g and κ in Eq.1 are consistent with a given experimental unpolarized angular distribution.

D. Determining κ

First we consider the experimentally allowed values of κ . The unpolarized angular distribution provides us with a range of values of ρ (Eq.12), but χ is unconstrained; we may combine this information through Eq.2 to determine the locus of allowed (complex) values of κ . This is shown in Fig.4.

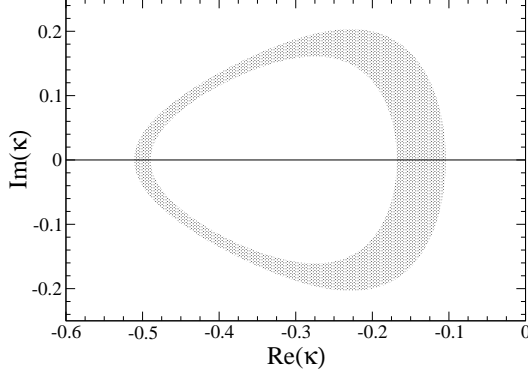


FIG. 4: The locus of complex κ (the $J/\psi p\bar{p}$ Pauli coupling) allowed by the experimental constraint $\rho = 0.726 \pm 0.074$, taken from the unpolarized differential cross section for $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$.

For $\chi = 0$, Eq.2 implies that κ is real and negative, and takes on the smallest allowed magnitude. As we increase χ from 0, the allowed κ values proceed clockwise, since κ initially acquires a negative imaginary part. The extreme values of κ on the real axis in Fig.4 are for $\chi = 0, \pi$, and are

$$\kappa = \begin{cases} -0.137 \pm 0.032, & \chi = 0 \\ -0.500 \pm 0.011, & \chi = \pi. \end{cases} \quad (13)$$

E. Determining g

Next we consider the determination of the overall $J/\psi \rightarrow p\bar{p}$ vertex strength g . Since the differential and total cross sections for $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$ only involve g through the ratio g/f_ψ , we must introduce additional experimental data to constrain g . The partial width for $J/\psi \rightarrow p\bar{p}$ is especially convenient in this regard, since it only involves the strong $J/\psi p\bar{p}$ vertex, and thus depends only on g and κ (and kinematic factors). This partial width was given in terms of the strong Sachs form factors in Eq.6; as a function of g and κ it is

$$\Gamma_{\psi \rightarrow p\bar{p}} = \frac{1}{3} \frac{g^2}{4\pi} M \sqrt{1-r} \left[1 + \frac{r}{2} + 3\Re(\kappa) + \left(1 + \frac{1}{2r}\right) |\kappa|^2 \right]. \quad (14)$$

This generalizes the $\kappa = 0$ result given in Eq.27 of Ref.[4] to a nonzero Pauli coupling. Using the PDG values [16] of $\Gamma_{J/\psi} = 93.4 \pm 2.1$ keV and $B_{J/\psi \rightarrow p\bar{p}} = (2.17 \pm 0.07) \cdot 10^{-3}$, Eq.14 implies a range of values of the overall vertex strength g for each value of the (unknown) phase χ . This is shown in Fig.5. There is a range of uncertainty in g at each χ (not shown in the figure), due to the experimental errors in $\Gamma_{J/\psi}$, $B_{J/\psi \rightarrow p\bar{p}}$ and ρ , which is at most $\sim \pm 5\%$.

Note that g is bounded by the limits at $\chi = 0$ and π , for which $g \approx 2.0 \cdot 10^{-3}$ and $\approx 3.4 \cdot 10^{-3}$ respectively. The allowed values of g are somewhat larger than our

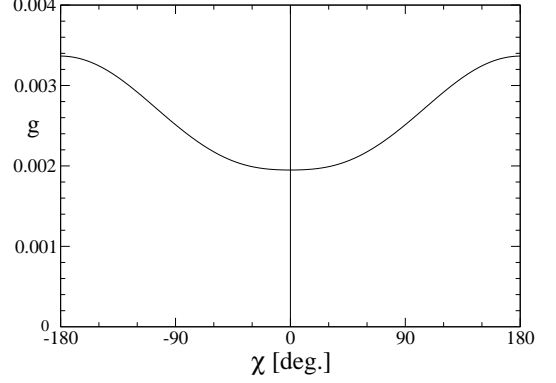


FIG. 5: The value of the overall $J/\psi p\bar{p}$ vertex strength g implied by the experimental $\Gamma_{J/\psi \rightarrow p\bar{p}}$ and ρ as a function of the unknown $J/\psi p\bar{p}$ Sachs phase χ .

previous estimate of $g = (1.62 \pm 0.03) \cdot 10^{-3}$ [4] assuming only a Dirac $J/\psi p\bar{p}$ coupling, as a result of destructive interference between the Pauli and Dirac terms.

IV. EFFECT ON $\sigma(p\bar{p} \rightarrow \pi^0 J/\psi)$

The effect of a $J/\psi p\bar{p}$ Pauli term on the $p\bar{p} \rightarrow \pi^0 J/\psi$ cross section may be of considerable interest for the PANDA project, since one might use this as a “calibration” reaction for associated charmonium production, and the Pauli term may be numerically important. Although we have carried out this calculation with the vertex of Eq.1 for general masses, the full result is rather complicated; here for illustration we discuss the much simpler massless pion limit.

For a massless pion the ratio of the unpolarized cross section $\langle \sigma(p\bar{p} \rightarrow \pi^0 J/\psi) \rangle$ with a Pauli term to the pure Dirac result (γ_μ only, denoted by D) is

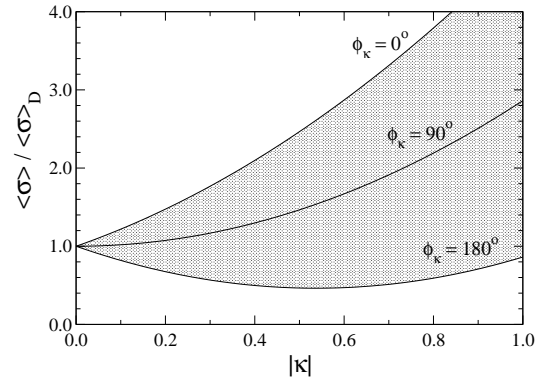


FIG. 6: The dependence of the unpolarized, near-threshold cross section $\langle \sigma(p\bar{p} \rightarrow \pi^0 J/\psi) \rangle$ on the (complex) Pauli coupling $\kappa = |\kappa|e^{i\phi_\kappa}$ (from Eq.15).

$$\frac{\langle \sigma(p\bar{p} \rightarrow \pi^0 J/\psi) \rangle}{\langle \sigma(p\bar{p} \rightarrow \pi^0 J/\psi) \rangle_D} \Big|_{m_\pi=0} = \left[1 + 2\Re(\kappa) + \left(\frac{1}{2} + \frac{M^2}{8m^2} \right) |\kappa|^2 \right. \\ \left. + \frac{(s - M^2)}{4m^2} \frac{\beta}{\ln[(1+\beta)/(1-\beta)]} |\kappa|^2 \right], \quad (15)$$

where $\beta = \sqrt{1 - 4m^2/s}$ is the velocity of the annihilating p and \bar{p} in the c.m. frame. The limit of this cross section ratio at threshold is shown in Fig.6 for a range of complex κ .

Evidently there is destructive interference for a κ with a dominant negative real part, as is suggested by the unpolarized data. For the value $\kappa = -0.50$ (the larger solution in Eq.13) there is roughly a factor of two suppression in the cross section over the prediction for a pure Dirac coupling. The suppression however depends strongly on the phase of κ , and for imaginary κ has become a moderate enhancement. Thus, the near-threshold cross section for $p\bar{p} \rightarrow \pi^0 J/\psi$ is quite sensitive to the strength and phase of the Pauli coupling; it will therefore be important for PANDA to have an accurate estimate of this quantity. In the next section we will show how both the magnitude and phase of κ can be determined in polarized $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$ scattering, and may be accessible at BES.

V. POLARIZATION OBSERVABLES

The relative phase χ of the $J/\psi p\bar{p}$ Sachs strong form factors \mathcal{G}_E and \mathcal{G}_M may be determined experimentally through a study of the polarized process $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$. As each of the external particles in this reaction has two possible helicity states, there are 16 helicity amplitudes in total. All the helicity amplitudes to the final $p\bar{p}$ helicity states $|p(\pm)\bar{p}(\pm)\rangle$ are proportional to \mathcal{G}_E , and all to $|p(\pm)\bar{p}(\mp)\rangle$ are proportional to \mathcal{G}_M . In the unpolarized case these are squared and summed, which leads to a cross section proportional to a weighted sum of $|\mathcal{G}_E|^2$ and $|\mathcal{G}_M|^2$. As we stressed earlier, this implies that the phase χ of $\mathcal{G}_E/\mathcal{G}_M$ is not determined by the unpolarized data.

To show how χ can be measured in polarized scattering, it is useful to introduce the polarization observables discussed by Paschke and Quinn [17]. These are angular asymmetries that arise when the polarizations of particles are aligned or anti-aligned along particular directions. For example, for our reaction $e^+e^- \rightarrow p\bar{p}$, $Q(0,0,z,0)$ is the difference of two angular distributions, $(d\sigma/d\Omega)_{p\uparrow} - (d\sigma/d\Omega)_{p\downarrow}$. Here we will use x and y for the two transverse axes and z for the longitudinal axis (see Fig.7). \hat{x} and \hat{z} vary with the particle, and \hat{y} is chosen to be common to all. An entry of 0 signifies an unpolarized particle. Since there are four possible arguments for each particle, 0, x , y and z , there are $4^4 = 256$ polarization

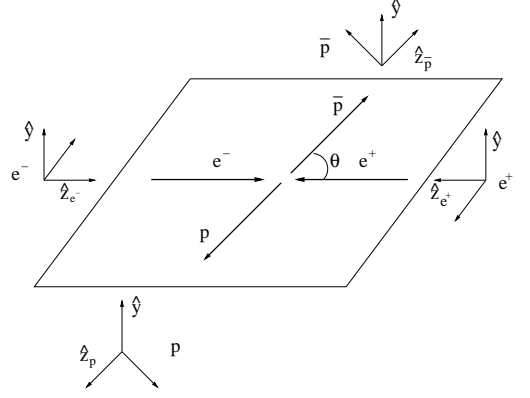


FIG. 7: Axes used to define the polarization observables.

observables for this process. Of course there is considerable redundancy, since they are all determined by the 16 helicity amplitudes. The constraints of parity and charge conjugation reduce this set to 6 independent helicity amplitudes, and for massless leptons (as we assume here) this is further reduced to 3 independent nonzero helicity amplitudes.

We introduce the normalized polarization observables $\mathcal{Q}_{\epsilon_e+\epsilon_{e-}\epsilon_{\bar{p}}\epsilon_p} \equiv Q(\epsilon_e+\epsilon_{e-}\epsilon_{\bar{p}}\epsilon_p) / Q(0,0,0,0)$, where $Q(0,0,0,0)$ is the unpolarized differential cross section. The (nonzero) polarization observables for this process satisfy the relations

$$\begin{aligned} (a) \quad & \mathcal{Q}_{0000} = \mathcal{Q}_{xxyy} = \mathcal{Q}_{yyyy} = -\mathcal{Q}_{zz00} = 1, \\ (b) \quad & \mathcal{Q}_{00y0} = \mathcal{Q}_{xx0y} = \mathcal{Q}_{yy0y} = \mathcal{Q}_{zz0y} = \\ & -\mathcal{Q}_{000y} = -\mathcal{Q}_{xx0y} = -\mathcal{Q}_{yy0y} = -\mathcal{Q}_{zz0y}, \\ (c) \quad & \mathcal{Q}_{xx00} = \mathcal{Q}_{yy00} = \mathcal{Q}_{00yy} = -\mathcal{Q}_{zzyy}, \\ (d) \quad & \mathcal{Q}_{z0x0} = \mathcal{Q}_{z00x} = \mathcal{Q}_{yxyz} = \mathcal{Q}_{yxzy} = \\ & -\mathcal{Q}_{0zx0} = -\mathcal{Q}_{0z0x} = -\mathcal{Q}_{xyyz} = -\mathcal{Q}_{xyzy}, \\ (e) \quad & \mathcal{Q}_{z0z0} = \mathcal{Q}_{0z0z} = \mathcal{Q}_{xyxy} = \mathcal{Q}_{yxxy} = \\ & -\mathcal{Q}_{0zz0} = -\mathcal{Q}_{z00z} = -\mathcal{Q}_{xyxy} = -\mathcal{Q}_{xyyx}, \\ (f) \quad & \mathcal{Q}_{xxxx} = \mathcal{Q}_{yyxx} = \mathcal{Q}_{zzzz} = -\mathcal{Q}_{00zz}, \\ (g) \quad & \mathcal{Q}_{00xx} = -\mathcal{Q}_{zzxx} = -\mathcal{Q}_{xxzz} = -\mathcal{Q}_{yyzz}, \\ (h) \quad & \mathcal{Q}_{00xz} = \mathcal{Q}_{xxzx} = \mathcal{Q}_{yyzx} = \mathcal{Q}_{zzzx} = \\ & -\mathcal{Q}_{xxxz} = -\mathcal{Q}_{yyxz} = -\mathcal{Q}_{zzxz} = -\mathcal{Q}_{00zx}, \\ (i) \quad & \mathcal{Q}_{xyx0} = \mathcal{Q}_{xy0x} = \mathcal{Q}_{z0yz} = \mathcal{Q}_{z0zy} = \\ & -\mathcal{Q}_{yx0x} = -\mathcal{Q}_{yx0x} = -\mathcal{Q}_{0zyz} = -\mathcal{Q}_{0zyz}. \end{aligned} \quad (16)$$

Explicit expressions for these observables are given in Table I.

The results in Table I suggest how we may determine χ experimentally. Inspection of the table shows that only four of the independent polarization observables depend

TABLE I: Nonzero inequivalent polarization observables in $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$. The function F is $4 - 2(1 - \rho^2) \sin^2 \theta$.

Pol. Observable	Result
\mathcal{Q}_{0000}	1
\mathcal{Q}_{00y0}	$4\rho \sin \chi \sin \theta \cos \theta / F$
\mathcal{Q}_{xx00}	$2(1 - \rho^2) \sin^2 \theta / F$
\mathcal{Q}_{z0x0}	$4\rho \cos \chi \sin \theta / F$
\mathcal{Q}_{z0z0}	$4 \cos \theta / F$
\mathcal{Q}_{00xz}	$-4\rho \cos \chi \sin \theta \cos \theta / F$
\mathcal{Q}_{xyx0}	$-4\rho \sin \chi \sin \theta / F$
\mathcal{Q}_{xxxz}	$[4 - 2(1 + \rho^2) \sin^2 \theta] / F$
\mathcal{Q}_{zzxz}	$-2(1 + \rho^2) \sin^2 \theta / F$

on χ ; two are proportional to $\sin \chi$ and two to $\cos \chi$. Assuming that one knows ρ with sufficient accuracy from the unpolarized data, one may then determine χ unambiguously by extracting $\sin \chi$ and $\cos \chi$ from the measurement of two of these polarization observables.

The determination of $\sin \chi$ is the most straightforward, since it only requires the detection of a single final polarized particle (for example the proton, through \mathcal{Q}_{00y0}). If κ is close to real, which corresponds to $\chi \approx 0$ or $\approx \pi$, this observable may be relatively small. The other polarization observables that are proportional to $\sin \chi$ involve asymmetries with either one or three particles polarized; these are given in relations (b) and (i) of Eq.16.

Determining $\cos \chi$ involves measuring double or quadruple polarization observables, which are given in relations (d) and (h) in Eq.16. In the double polarization case, either one initial and one final polarization are measured (such as e^- and p) or the polarizations of both final particles (p and \bar{p}) are measured. In the first case the relevant observables (such as \mathcal{Q}_{z0x0}) require the initial lepton to have longitudinal ($\pm \hat{z}$) polarization, which is difficult to achieve experimentally. In the second case the initial e^+e^- beams are unpolarized, and the longitudinal polarization of one final particle and the transverse polarization of the other must be measured. Determining the \bar{p} polarization may prove to be an experimental challenge.

Of these two general possibilities, the most attractive “next experiment” beyond unpolarized $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$ scattering may be a measurement of the differential cross section with unpolarized leptons and only the final p polarization detected. This will determine $\sin \chi$, which specifies χ up to the usual trigonometric ambiguities.

Another interesting experimental possibility is to resolve the phase ambiguity in unpolarized $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$ scattering through a study of the closely related reaction $e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}$, which has recently been observed by BABAR [18] using the ISR technique. Since the $\psi p\bar{p}$ and $\psi \Lambda\bar{\Lambda}$ couplings are identical in the SU(3) flavor symmetry limit, a determination of $J/\psi \Lambda\bar{\Lambda}$ couplings

would suggest plausible $J/\psi p\bar{p}$ couplings. This approach has some experimental advantages; as the Λ and $\bar{\Lambda}$ decays are self-analyzing, no rescattering of the final baryons is required to determine their polarization. In addition no beam polarization is required, since it suffices to measure the (odd- ρ) polarization observables \mathcal{Q}_{00y0} and \mathcal{Q}_{00xz} . One may also measure the even- ρ observables \mathcal{Q}_{00xx} and \mathcal{Q}_{00zz} as a cross-check of the result for ρ .

Finally, we note in passing that it may also be possible to measure the appropriate polarization observables in the time-reversed reaction $p\bar{p} \rightarrow J/\psi \rightarrow e^+e^-$.

VI. SUMMARY AND CONCLUSIONS

The unpolarized angular distribution for the process $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$, measured recently by the BES Collaboration, is inconsistent with theoretical expectations for a pure Dirac $J/\psi p\bar{p}$ coupling. In this paper we have derived the effect of an additional Pauli-type $J/\psi p\bar{p}$ coupling, and find that this can accommodate the observed angular distribution. The $J/\psi p\bar{p}$ Pauli coupling may significantly affect the cross section for the charmonium production reaction $p\bar{p} \rightarrow \pi^0 J/\psi$, which will be studied at PANDA. There is an ambiguity in determining the relative Dirac and Pauli $J/\psi p\bar{p}$ couplings from the unpolarized $e^+e^- \rightarrow J/\psi \rightarrow p\bar{p}$ data; we noted that this ambiguity can be fully resolved through measurements of the polarized reaction. The most attractive polarized process to study initially appears to be the case of unpolarized initial e^+e^- beams, with only the final p (transversely) polarized. Alternatively, measurement of the required polarization observables may also be possible using the time-reversed reaction $p\bar{p} \rightarrow J/\psi \rightarrow e^+e^-$. It may also be possible to use self-analyzing processes such as $e^+e^- \rightarrow J/\psi \rightarrow \Lambda\bar{\Lambda}$ to estimate the Dirac and Pauli couplings in the closely related $J/\psi \Lambda\bar{\Lambda}$ vertex.

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